



Restoration of eastern oyster populations with positive density dependence

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Abstract. Positive density dependence (i.e., Allee effects) can create a threshold of population states below which extinction of the population occurs. The existence of this threshold, which can often be a complex, multi-dimensional surface, rather than a single point, is of particular importance in degraded populations for which there is a desire for successful restoration. Here, we incorporated positive density dependence into a closed, size- and age-structured integral projection model parameterized with empirical data from an eastern oyster, *Crassostrea virginica*, population in Pamlico Sound, North Carolina, USA. To understand the properties of the threshold surface, and implications for restoration, we introduced a general method based on a linearization of the threshold surface at its unique, unstable equilibrium. We estimated the number of oysters of a particular age (i.e., stock enhancement), or the surface area of dead shell substrate required (i.e., habitat enhancement) to move a population from an extinction trajectory to a persistence trajectory. The location of the threshold surface was strongly affected by changes in the amount of local larval retention. Traditional stock enhancement with oysters <1 yr old (i.e., spat) required three times as many oysters relative to stock enhancement with oysters between ages 3 and 7 yr old, while the success of habitat enhancement depended upon the initial size distribution of the population. The methodology described here demonstrates the importance of considering positive density dependence in oyster populations, and also provides insights into effective management and restoration strategies when dealing with a high dimensional threshold separating extinction and persistence.

Key words: *Crassostrea virginica*; habitat enhancement; integral-projection model; oyster demography; oyster restoration; positive density dependence; stock enhancement.

INTRODUCTION

Many natural populations exhibit positive density dependence, or Allee effects, in which an increase in population size leads to an increase in per capita growth rate, or other components of fitness (Allee 1931, 1949, Courchamp et al. 1999, Stephens et al. 1999). These Allee effects arise through various mechanisms, such as mate limitation or predator saturation (Courchamp et al. 1999, Schreiber 2003, Gascoigne and Lipcius 2004). Positive density dependence might also arise in populations of ecosystem engineers, organisms that significantly modify the surrounding abiotic and biotic environment, as the population size must be sufficiently large to generate required environmental change for population persistence (Byers et al. 2006, Cuddington et al. 2009). If the Allee effect is strong enough, at low population sizes the population will experience negative growth rates and ultimately extinction (Courchamp et al. 1999). This leads to a critical population size required for population persistence; below this critical threshold, the population will decline to extinction, while above this threshold, the population will persist. Knowledge of this critical threshold is thus of particular importance in exploited or degraded

populations where there is an interest in population restoration or conservation (Courchamp et al. 2008).

One ecosystem engineer of particular restoration importance is the eastern oyster, *Crassostrea virginica*. This species inhabits thousands of miles of coastline, and provides valuable ecosystem services, including commercial harvest, water filtration, shoreline stabilization, erosion protection, and habitat and predator refuge for a variety of organisms (Coen et al. 2007, Grabowski et al. 2012). In these oyster populations, individuals aggregate into large, complex reef structures. Reefs are composed of living oysters, as well as oyster shell that remains following natural mortality. Shell, both living and dead, provides solid substrate on which new oyster larvae can attach, increasing larval survival by providing shelter from predators and preventing burial in sediment (Rothschild et al. 1994, Mann and Powell 2007). Reefs also increase growth and survival of adult oysters by increasing water filtration, buffering against hypoxic events, and increasing food availability through increased current speeds (Lenihan et al. 1996, Lenihan and Peterson 1998, Bartol et al. 1999, Lenihan 1999, Schulte et al. 2009).

Globally, oysters have experienced severe population declines due to decades of overfishing, coastal development, and pollution (Airoldi and Beck 2007, Beck et al. 2011). Particularly damaging has been the use of destructive fishing practices that not only remove older, more fecund individuals, but also destroy the reef structure and available substrate that is necessary for recruitment and persistent populations (Rothschild et al. 1994). Additionally, the emergence and

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increasing prevalence of two protozoan diseases, MSX and Dermo, along the eastern United States in the mid to late 1900s has contributed to population declines (Hofmann et al. 2009, Carnegie and Burreson 2011). Along the eastern coast of the United States, many native *C. virginica* populations have been reduced to <15% of their historic population sizes, with an associated decline in substrate availability and integrity (Rothschild et al. 1994, Beck et al. 2011, Wilberg et al. 2011, zu Ermgassen et al. 2012).

Demographic modeling has shown that positive feedbacks between living oysters and shell substrate can lead to thresholds between population persistence and extinction, as well as possible alternative stable states (Jordan-Cooley et al. 2011, Nystrom et al. 2012, Housego and Rosman 2016). In systems with alternative stable states, restoration becomes particularly challenging as transitions between desired and undesired states can occur through sudden, often unpredictable, phase shifts, and successful restoration often requires the conditions of the system be returned to levels more extreme than those immediately prior to the phase shift (Scheffer et al. 2001, Beisner et al. 2003, Scheffer and Carpenter 2003, Hastings and Wysham 2010). In oysters, the desirable state consists of a healthy, abundant population of oysters on high-relief reefs, while the undesirable state is heavily degraded, with low or zero population sizes.

Empirical data, field experiments, and restoration efforts also support the concept of alternative stable states and the importance of reef height on persistence (Powell et al. 2009a, b, Schulte et al. 2009, Lipcius et al. 2015, Colden et al. 2017). For example, Powell et al. (2009b) analyzed a time series of *C. virginica* populations in Delaware Bay from 1953 to 2006 and found that the population persisted for extended periods of time in two distinct states, one of high abundance, and one of low abundance. Additionally, Schulte et al. (2009) and Lipcius et al. (2015) showed that the success of restoration of *C. virginica* populations in two tributaries of the Chesapeake Bay was influenced significantly by the vertical height of the reef. Locations restored with high vertical reefs had greater oyster densities and were likely to persist, while populations restored with low vertical reefs had low oyster densities and were predicted to decline to extinction within a handful of years. In field experiments, Colden et al. (2017) demonstrated a threshold reef height above which oyster reefs persisted and below which the reefs degraded to local extinction. These results indicate that a critical threshold of reef height is required for persistence.

Given the possible existence of a threshold between population persistence and extinction, it is important to understand the shape of this threshold in size-structured populations, and what restoration actions can be taken to push a population from an extinction trajectory to a persistent trajectory. Restoration efforts in oyster populations generally consist of (1) stock enhancement, i.e., supplementing existing populations with additional oyster spat reared in the lab, and transplanting oysters from protected populations or oysters grown in aquaculture-like "oyster gardens"; (2) habitat enhancement, i.e., adding recycled shells or artificial reef structures to increase the availability of substrate; or (3) a combination of stock and habitat enhancement (Brumbaugh and Coen 2009). While there has been successful restoration of some *C. virginica* populations along the mid-Atlantic U.S.

coast (Taylor and Bushek 2008, Powers et al. 2009, Schulte et al. 2009, Puckett and Eggleston 2012, Lipcius et al. 2015), there are concerns about the efficacy of alternative restoration actions, and there is no current agreement on the best approaches for achieving success (Kennedy et al. 2011, Gerardi et al. 2013, Baggett et al. 2014, Lipcius et al. 2015, Puckett and Eggleston 2016).

Here, we use *C. virginica* as a model species to investigate the impact of positive density dependence on population dynamics and restoration actions. Specifically, we are interested in understanding the properties of the threshold between population persistence and extinction. We extend a closed, size- and age-structured integral projection model (IPM) developed in Moore et al. (2016) to include a positive feedback between the establishment of new oyster larvae and shell substrate. We use this model to address several questions. First, we explore properties of the threshold and introduce a general analytic method for approximating the infinite dimensional threshold surface. We next investigate the effect of population size structure on the threshold surface, and the ultimate fate of the population. Finally, we assess the relative effectiveness of two restoration actions, namely stock enhancement using oysters of different ages, or habitat enhancement, for recovery of a population declining toward extinction.

METHODS

Model

We extend an age- and size-structured integral-projection model (IPM) developed in Moore et al. (2016). Fig. 1 shows a simplified representation of the full model. Briefly, let $n_a(x, t)dx$ be the density of age a , size x oysters at time t , with x measured as the shell length of an oyster in mm. Oysters of size x will survive to the next time step and grow to size y according to age- and size-specific survival and growth kernels, $S_a(x)$ and $G_a(y, x)$, respectively. The fecundity kernel, $F_a(y, x, H(t) + L(t))$, represents the density of size y recruits produced by an adult of age a and size x . The fecundity kernel also depends upon, $H(t)$, the m^2 of dead shell substrate available at time t , and $L(t)$, the m^2 of living shell substrate available at time t . Though adult oysters are also positively affected by the amount of substrate (Lenihan and Peterson 1998, Lenihan 1999, Jordan-Cooley et al. 2011), for simplicity we do not consider that effect here.

The dynamics of the population are expressed as

$$n_1(y, t + 1) = \sum_{a=2}^A \int_0^U S_a(x) F_a(y, x, H(t) + L(t)) n_a(x, t) dx + \sum_{a=2}^A S_a(U) F_a(y, U, H(t) + L(t)) B_a(t) \quad (1)$$

$$n_{a+1}(y, t + 1) = \int_0^U S_a(x) G_a(y, x) n_a(x, t) dx \quad \text{for } a \geq 1 \quad (2)$$

where A is the maximum age of an individual and U is the maximum size of an individual. To avoid artificial eviction of individuals growing larger than the maximum size, $B_a(t)$ is the

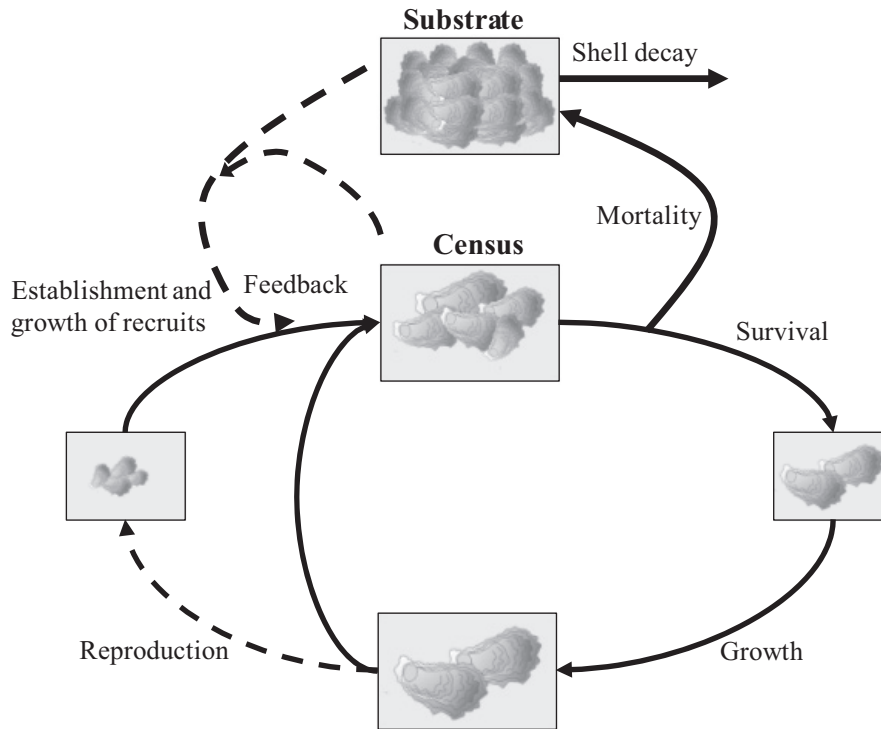


FIG. 1. Representation of model. Census occurs immediately following summer recruitment. Oysters then experience mortality, with dying oysters converted to a surface area of substrate. Surviving oysters grow before reproducing. Following reproduction, new oyster recruits experience a separate growth event before joining existing oysters immediately prior to the next census. The number of recruits that successfully establish depends upon the degree of local retention, and the feedback with substrate, which is composed of the surface area of both living and dead shells.

density of a discrete size class for individuals of size $x > U$ whose kernels for survival and fecundity are set equal to kernels for individuals of size $x = U$ (Williams et al. 2012, Moore et al. 2016). The dynamics of these discrete classes are given by

$$B_{a+1}(t + 1) = \int_0^U S_a(x)n_a(x, t) \int_U^\infty G_a(y, x)dydx + B_a(t)S_a(U) \quad \text{for } a \geq 1 \quad (3)$$

with $B_1(t) = 0$ for all t . The dynamics of dead shell substrate is given by

$$H(t + 1) = H(t)e^{-\delta} + \sum_{a=1}^A \left[\int_0^U k_1 x^{k_2} [1 - S_a(x)]n_a(x, t)dx + k_1 U^{k_2} (1 - S_a(U))B_a(t) \right] \quad (4)$$

where δ is the decay rate of dead shell (per year), and k_1 and k_2 are scaling parameters that convert the number of size x individuals to square meters of surface area.

In Pamlico Sound, spawning of *C. virginica* is protracted, with a primary spawning and settlement peak in May and June, and a secondary spawning and settlement peak in July and August (Ortega and Sutherland 1992, Mroch et al. 2012). For simplicity, we model reproduction as occurring once at the end of the spring, with census occurring immediately thereafter. Between reproduction and census, adult oysters experience mortality, then grow from their current size x

to their final end-of-year size, x' . The surface area of substrate due to living and recently deceased oysters equals

$$L(t) = \sum_{a=1}^A \int_0^U \left[(1 - S_a(x))k_1 x^{k_2} + S_a(x) \int_0^U (G_a(x', x)k_1 (x')^{k_2}) dx' \right] n_a(x, t)dx + \sum_{a=1}^A k_1 U^{k_2} B_a(t). \quad (5)$$

Reproduction occurs according to a size-specific fecundity relationship, $f(x', H(t) + L(t))$. This fecundity relationship is composed of two parts: (1) the number of new oyster larvae that are produced, survive, and settle in the natal population and (2) the feedback between total available substrate and the fraction of larvae that are able to successfully establish. We assume the number of eggs produced is dependent upon the size of the parent and that all oyster recruits are created by adults of the local population (i.e., there is no immigration). The fecundity relationship is given by

$$f(x', H + L) = v(x')m(x')\rho \frac{H + L}{\alpha + H + L} \quad (6)$$

where $v(x')$ is the proportion of size x' individuals in the population that are female, $m(x')$ is the number of eggs produced by a size x' individual, ρ is the maximal local retention of oyster larvae (e.g., the proportion of eggs that survive and settle in the natal population), and $(H + L)/(\alpha + H + L)$

represents the positive feedback between available substrate and recruitment. The sizes of the newly recruited oysters are assumed to be normally distributed with density $z(y)$. Thus, the overall fecundity kernel is expressed as

$$F_a(y, x, H + L) = \begin{cases} \frac{H+L}{\alpha+H+L} \rho z(y) \left(\int_0^U v(x') m(x') G_a(x', x) dx' \right. \\ \left. + v(U) m(U) \int_U^\infty G_a(x', x) dx' \right) & \text{if } x < U \\ \frac{H+L}{\alpha+H+L} \rho z(y) v(U) m(U) & \text{if } x \geq U. \end{cases} \quad (7)$$

While there is evidence that a combination of positive and negative density dependence is important in oyster systems, potentially leading to alternative stable states (Powell et al. 2009b, Knights and Walters 2010, Jordan-Cooley et al. 2011, Puckett and Eggleston 2012), here we are only interested in what determines population persistence vs. extinction, rather than the properties of the system at some stable carrying capacity. As such, we restrict our focus to investigating the effects of positive density dependence, rather than the effects of both positive and negative density dependence.

Data

We estimated site-specific kernels for growth, survival, and fecundity using data collected from the West Bay *C. virginica* population in Pamlico Sound, North Carolina, USA. A full description of the methods is provided in Mroch et al. (2012) and Puckett and Eggleston (2012, 2016). Briefly, data to estimate growth and survival kernels were obtained by deploying 15 replicate settlement trays at a single restored oyster reef protected from harvest. On each tray, individual settlers were marked and growth and mortality tracked from June 2006 to October 2008. To estimate size-specific per capita fecundity, oysters were collected from the reef and brought back to the lab to determine the total egg content of each oyster following the general procedures of Cox and Mann (1992).

Statistical fitting

Growth and survival kernels.—To estimate the growth kernel, $G_a(y, x)$, we fit a linear regression of the log change in size from time t to $t + 1$ against the size at time t , assuming constant variance across all ages and sizes. Fitting growth in this way ensures non-negative changes in size, which is important for describing oyster growth (Moore et al. 2016). We fit the survival kernel, $S_a(x)$, using logistic regression of survival between years. We assume that mortality is age and size dependent, with larger, older oysters more susceptible to diseases and juveniles more susceptible to predation. While we do not measure these effects explicitly, we assume these processes are captured implicitly in the field data.

Fecundity kernel.—We estimate the size-specific number of eggs produced, $m(x')$, with a scaling relationship. Using the estimated number of eggs produced during May 2007 and May 2008 (Mroch et al. 2012), we fit a linear relationship

between the log number of eggs and log oyster size. Since oysters are protandric hermaphrodites, beginning life as male and switching to female at larger sizes (Galtsoff 1964), we expect a higher proportion of females at larger sizes. We thus estimate the size-specific proportion of females in the population, $v(x')$, with a linear regression of the proportion of females in the population against size, using data from May 2007 and May 2008 (Mroch et al. 2012). After fitting the model, we bound the function such that any negative value was set equal to zero, while any value greater than one was set equal to one. However, model results are not highly sensitive to the form chosen for $v(x')$. We estimate the size distribution of new recruits, $z(y)$, with a normal distribution, using the mean and standard deviation of measured recruit sizes from August 2006 and August 2007 (Puckett and Eggleston 2012).

Local retention, ρ , depends upon factors such as fertilization success, survival during the pelagic larval stage, predation, and local dispersal and transport processes. Here, we parameterize ρ using results of a coupled hydrodynamic and particle tracking simulation presented in Puckett et al. (2014). Briefly, larval dispersal was simulated over a 21-d period, whereby a daily instantaneous mortality rate of 0.2 per day was applied. After 14 d, larvae were assumed to settle if located within the reef polygon. Local retention was estimated as the proportion of larvae spawned from a reef that settled within their natal reef. We also consider the case when local retention is low. For this case, we set ρ to 50% above the minimum value of local retention that still yields a positive equilibrium (Appendix S1).

Finally, to estimate the α parameter of the positive feedback function, we solve for α using Eq. 6 multiplied by $n(x')$. Thus

$$\alpha = \frac{v(x') m(x') n(x') \rho (H(t) + L(t))}{r} - H(t) - L(t) \quad (8)$$

where r is the observed, size-independent number of recruits. We obtain estimates of r , $n(x')$, $H(t)$, and $L(t)$ from Puckett and Eggleston (2012). Estimates of $v(x')$, $m(x')$, and ρ are as described above.

Substrate dynamics.—We obtain estimates of dead shell decay rate, δ , from Wilberg et al. (2013). For k_1 and k_2 , the scaling parameters between oyster length and surface area, we used the scaling relationship given in Galtsoff (1966).

Model analysis

To understand the dynamics of the model, we first assess model behavior by analytically approximating the location of the threshold surface dividing regions of population persistence from regions of population extinction. We then conduct an elasticity analysis to determine how the location of this threshold surface is affected by changes in model parameters. Finally, we assess several restoration scenarios using these analytic approximations and numerical simulations.

Model behavior.—The theory developed in Schreiber (2004) applies to the discretization of the IPMs that are used for all our numerical work. This theory characterizes the dynamical

behavior of the model using the dominant eigenvalue of the model at low densities, λ_0 , and the dominant eigenvalue at high densities, λ_∞ . Using these eigenvalues, there are three possible dynamics: (1) asymptotic extinction for all initial densities when $\lambda_\infty < 1$; (2) unbounded growth (persistence) for all non-zero initial densities when $\lambda_0 > 1$; and (3) the existence of a co-dimension one threshold surface such that initial conditions below this surface lead to extinction, while initial conditions above this surface lead to unbounded growth (persistence). For the parameters considered here, the model always exhibits the third behavior. Moreover, as we will show, there is a unique unstable equilibrium on this threshold surface. We use linearization at this unstable equilibrium to gain insights into the geometry of the threshold surface.

At the unstable equilibrium on the threshold surface, the dominant eigenvalue, λ , of the demographic transition operator equals one. We use this property, and results from the linear model with no positive feedbacks, to solve for the equilibrium value of dead shell substrate, \hat{H} , the total number of oysters at equilibrium across all ages and sizes, \hat{N} , the amount of living shell substrate at equilibrium, \hat{L} , and the stable size and age distribution when $\lambda = 1$ in the linear model with no positive feedbacks, $\hat{n}_a(x)$. Details of this analysis, and the resulting equilibrium equations, are provided in Appendix S1.

To investigate model behavior around the unstable equilibrium, we run simulations of population trajectories using two initial size and age distributions: (1) the equilibrium size and age distribution, $\hat{n}_a(x)$, and (2) a harvested age and size distribution, set by truncating and re-normalizing the equilibrium size and age distribution such that all oysters ≥ 75 mm shell length were removed from the population. While fishing mortality is rarely 100%, studies in Pamlico Sound have shown that the average number of legal-sized oysters in harvested populations can be as low as 93% less than the average number of legal-sized oysters in non-harvested populations (Puckett and Eggleston 2012, Peters et al. 2017). Thus, the harvested distribution used here roughly approximates a worst-case scenario of a population experiencing severe harvesting pressure. For each of the two initial size and age distributions, we numerically estimate the total oyster numbers and dead shell above which the population would persist, and below which the population would decline to extinction. We do this using a bisection search algorithm. Briefly, we first set the initial amount of dead shell, H_0 . We then determine an initial value of total oysters, c_1 , such that a population beginning at this value is above the threshold surface and persists, and an initial value of total oysters, c_2 , such that a population beginning at this value is below the threshold surface and goes extinct. We then run the simulation with an initial total oyster number equal to $c_3 = (c_1 + c_2)/2$. If this new population is above the threshold surface, in the next simulation we set the new total oyster number equal to $c_4 = (c_2 + c_3)/2$, otherwise we set the new total oyster number equal to $c_4 = (c_1 + c_3)/2$. We repeat this process k steps until c_k is above the threshold surface and $c_k - c_{k-1} < 0.001\hat{N}$. We repeat this process across a range of values of H_0 near \hat{H} and for each of the two initial size and age distributions.

Elasticity analysis.—Given that many parameters of the model are highly uncertain, and potentially variable across space and time, we compute the elasticity of the equilibrium

to local retention, ρ , the shape parameter of the feedback function, α , and the dead shell decay rate, δ . These elasticities indicate the percentage change in the equilibrium values given a 1% change in the parameter. Appendix S2 gives the specifics of calculating the elasticity of the equilibrium population densities to δ , ρ , and α .

Restoration scenarios and analytic approximations.—Restoration of an oyster population is desirable if the population lies below the threshold surface and is heading toward extinction. Successful restoration is then defined here as restoration actions that push the population across the threshold surface such that the population will theoretically increase toward infinity. Here, we consider two types of pulse restoration actions: (1) the addition of cohorts of oysters of a single age, a and (2) the addition of dead shell. Since restoration actions require significant amounts of time and money, we are interested in determining the minimum amount of either oysters or dead shell that will push the population across the equilibrium threshold surface. We approach this question using an analytic approximation for oyster additions, and numerically for both oyster or dead shell additions.

First, we investigate the linearization of the threshold surface around the unstable equilibrium (Appendix S3). The left dominant eigenvector of this operator gives the direction perpendicular to the threshold surface, and thus indicates the relative amount of oysters of a particular age and size that should be added to minimize the distance between the threshold surface and a point below the threshold surface (Appendix S4). Since we are interested in adding cohorts of oysters of a particular age to better reflect restoration practices, we use the relationship between the left eigenvector, the unstable equilibrium, and the size distribution of age a oysters to analytically approximate the total number of age a oysters required to cross the threshold surface (Appendix S4). We determined the size distribution of age a oysters by applying the growth and survival kernels to the initial distribution of age 1 recruits, $z(y)$, and re-normalizing the distribution after each time step.

To determine whether the analytic approximations of the required oyster numbers work well, we also simulate restoration actions numerically to determine the minimum number of age a oysters, or the minimum amount of dead shell required to push the population over the threshold surface, assuming a one-time addition of either substrate or oysters of age a . To numerically determine the minimum number of oysters of age a or dead shell required, we use the bisection search algorithm described in *Methods: Model analysis*. For simulations of oyster additions, we assume the population starts with no living oysters, and no available dead shell. This assumes a worst-case scenario in which an oyster population once existed, but became degraded to the extent that no oysters or shell remain. For dead shell additions, we assume the population starts with no available dead shell substrate, and a number of oysters equal to 10% above or 10% below \hat{N} . Given that these initial populations contain oysters, there will be some living shell substrate on which oyster larvae can settle. We modeled the size distribution of existing oysters using either the equilibrium size distribution, or the harvested size distribution.

In all model analyses, we discretized the integral operators using the midpoint rule with 250 equally sized bins from size 0 to 250 mm, for each age class from 0 to 10 yr. We ran all simulations for 150 time steps, with one time step equal to one year. Model implementation and data analysis were conducted with R (R Core Team, 2015).

RESULTS

Statistical fits

A total of 590 oysters were observed for approximately 2 yr post-settlement from June 2006 to October 2008. Measured oyster sizes ranged from 5.4 mm to 86.1 mm, while oyster ages ranged from 62 d to 2.3 yr. Oyster sizes observed from quadrat sampling (to obtain individuals to estimate per-capita fecundity) ranged from 6 to 124 mm on substrate that was 3–5 yr old over the course of the study (Mroch et al. 2012, Puckett and Eggleston 2012). In the model, we extrapolated both size and age to span a biologically realistic range of values, allowing size to vary from 0 mm to 250 mm, and age to vary from 0 d to 10 yr.

While previous work has shown the importance of including both age- and size-structure in models of oyster populations (Moore et al. 2016), the limited time-frame of our data led to poor fits for growth and survival functions when including both age and size. We thus fit growth and survival functions using only size, but also included a maximum age of survival, $A = 10$, beyond which no oysters survive, regardless of size. The final growth function shows a negative relationship between the log change in size and size of an oyster. When translated to the relationship between size at time $t + 1$ and size at time t , this led to a growth function in which oyster growth slowed as size increased (Fig. 2A). Oyster survivorship increased as a function of size (Fig. 2B).

The proportion of females in the population increased as a function of size (Fig. 3A), while the log number of eggs increased linearly as a function of log female size (Fig. 3B).

The size distribution of new recruits was normally distributed with mean \pm SD of 16.47 ± 5.50 mm (Fig. 3C).

We set the degree of local retention $\rho_{\text{est}} = 2.617898 \times 10^{-3}$, using estimates from Puckett and Eggleston (2016). We also investigated model results when the degree of local retention was low (for instance, if environmental conditions changed such that recruit survivorship decreased), and set $\rho_{\text{low}} = 2.842991 \times 10^{-5}$. This value was chosen to be equal to 50% above $\hat{\rho}$, the minimum value of local retention that still yields a positive equilibrium. To find the unstable equilibrium, we used a value of $\hat{\rho} = 1.89532724809747 \times 10^{-5}$, which yielded a long-term population growth rate of $\lambda = 1.0000000000923$ in the linear model.

To obtain an estimate of α , we used $H = 4,134.5$ m² and $L = 5,022.058$ m² (Puckett and Eggleston 2012), and a total population size of $N = 3,583,233.333$ oysters (Puckett and Eggleston 2016). We multiplied the total population size by size-frequency data of oysters at this location to obtain an estimate of the size distribution $n(x)$ (Puckett and Eggleston 2016). To estimate r , we used the number of observed recruits in August 2006 to obtain an estimate of $r = 4,266,804$ new recruits (Puckett and Eggleston 2012). Since r , as estimated in Puckett and Eggleston (2012), measures the overall number of recruits, it is possible that this value includes immigrant recruits produced from outside the local population. However, as the West Bay site is relatively isolated from other nearby oyster reefs, the input of oyster recruits from external sources is likely small (Puckett and Eggleston 2016). Plugging these values, as well as ρ_{est} and size-specific sex ratios and eggs as described above, into Eq. 7 yielded a value of $\alpha = 48,280.45$.

Wilberg et al. (2013) gives a range of shell decay rates from 0.05 to 0.4 per year. We used a mid value from this range and set $\delta = 0.2$. We also explored dynamics for values of δ at the extremes of this range. Galtsoff (1966) give the scaling relationship between oyster length, in cm, and surface area, in cm², as $1.25 (L_{\text{cm}})^{1.56}$. Converting to mm and m², respectively, yields $k_1 = 3.443 \times 10^{-6}$ and $k_2 = 1.56$, and thus area = $3.443 \times 10^{-6} (L_{\text{mm}})^{1.56}$ m².

All demographic functions and parameter estimates are given in Table 1.

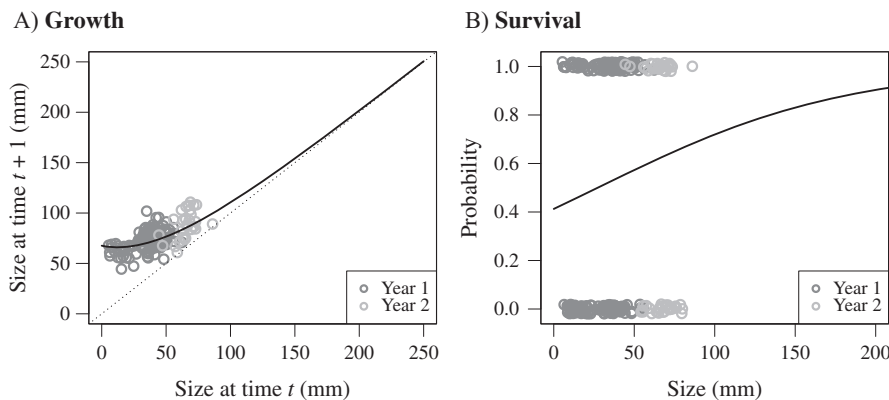


FIG. 2. Growth and survival functions. Statistical fits of (A) size-dependent growth and (B) survival functions. (A) Growth functions are fit using linear regression on the log change in size against size, then translated to generate the relationship between size at time $t + 1$ and size at time t . The dotted black diagonal line is the 1:1 line. (B) Survival functions are fit using linear regression of survival between time points. All functions are extrapolated past the collected data (gray points) to the minimum (0 mm) and maximum (250 mm) sizes. Model parameters are given in Table 1.

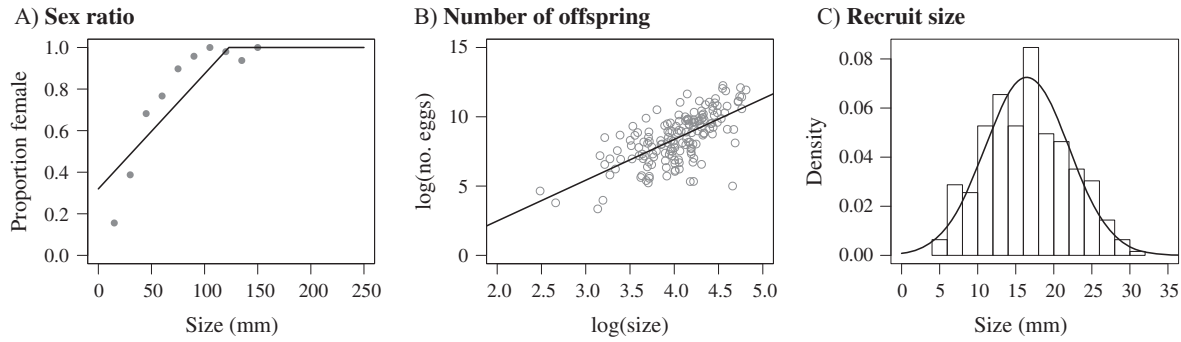


FIG. 3. Fecundity functions. (A) The proportion of females as a function of size. (B) The log number of eggs produced as a function of log female size. (C) The distribution of offspring size, fit to August 2007 and 2008 recruit sizes. Data for panels A and B are from Mroch et al. (2012), and data for panel C is from Puckett and Eggleston (2012). Parameters of all model fits are given in Table 1.

Model analysis

Model behavior.—Using the parameter values in Table 1, the unstable positive equilibrium is $(\hat{N}, \hat{H}) = (40, 329.56)$ oysters, 207.10 m^2 when ρ is high (ρ_{est}), and $(\hat{N}, \hat{H}) = (11,060, 285.35)$ oysters, $56,796.91 \text{ m}^2$ when ρ is low (ρ_{low}). For ρ_{est} , $\hat{L} = 144.99 \text{ m}^2$, and for ρ_{low} , $\hat{L} = 39,763.98 \text{ m}^2$. To visualize the threshold surface, we plotted population trajectories and slices of the threshold surface in the plane of total oyster and dead shell densities (Fig. 4A). The slice of the threshold surface corresponding to the equilibrium size distribution (Fig. 4B) passes through the unstable equilibrium, while the slice of the threshold surface corresponding to the harvested size distribution (Fig. 4C) lies above the unstable equilibrium. Above the slice for the harvested size distribution (Fig. 4A, region I), populations beginning at either initial size distributions will increase to infinity. Below the slice for the equilibrium distribution (Fig. 4A, region III) populations beginning at either initial size distribution will decline to extinction. However, there exists a large region between the two threshold slices (Fig. 4A, region II), where populations beginning at the equilibrium size distribution will increase to infinity, but

populations beginning at the harvested size distribution will decline to extinction, even if the population begins above (\hat{N}, \hat{H}) . Additionally, populations beginning at the harvested size distribution will often exhibit complex, oscillatory behavior during the first 10–12 yr of the simulation, regardless of whether they are declining toward extinction or increasing toward infinity.

Elasticity analysis.—Increasing the feedback parameter, α , will increase \hat{x} , while increasing local retention, ρ , will decrease \hat{x} (Fig. 5). Increasing the substrate decay rate, δ , will increase \hat{N} and decrease \hat{H} , though the effect on \hat{H} is much smaller than the effect on \hat{N} (Fig. 5). Of the three parameters, changes in local retention ρ has the largest impact on the threshold surface, while changes in δ has the smallest impact on the threshold surface. The effect on \hat{x} to changes to ρ is reduced when ρ is high, while the effect on \hat{x} to changes to δ is reduced when δ is low (not shown).

Restoration scenarios.—Fig. 6 shows the normalized size distributions of age a oysters. Using these distributions and

TABLE 1. Demographic functions and parameter estimates of statistical models and parameter estimates for the size- and age-structured model used to describe *C. virginica* demography.

Demographic process	Model/Parameter	References
Growth	$\hat{y} = 4.213(0.091) - 0.019(0.002)x$ Standard deviation about the growth curve, $\sigma = 0.421(0.025)$	Puckett and Eggleston (2012)
Survival	$\text{logit}(s) = -0.353(0.273) + 0.013(0.006)x$	Puckett and Eggleston (2012)
Fecundity		
Sex ratio	$v(x) = 0.320(0.106) + 0.006(0.001)x$	Mroch et al. (2012)
log(no. eggs)	$\text{log}(m(x)) = -3.409(1.064) + 2.944(0.262)\text{log}(x)$	Mroch et al. (2012)
Distribution of recruit sizes	$z(y)$, Gaussian with mean = 16.472, variance = 30.237	Puckett and Eggleston (2012)
Feedback		
Local retention, linear model	$\hat{\rho} = 1.89533 \times 10^{-5}$ [$\lambda = 1.00000000000923$]	estimated from model
Local retention, nonlinear model	$\rho_{\text{est}} = 2.618 \times 10^{-3}$, $\rho_{\text{low}} = 2.843 \times 10^{-5}$	Puckett and Eggleston (2016)
Shape parameter	$\alpha = 48,280.45$	estimated from model and Puckett and Eggleston (2012)
Shell parameters		
Decay rate (per year)	$\delta = 0.2$	Wilberg et al. (2013)
Scaling relationship	surface area (m^2) = $3.443 \times 10^{-6} x^{1.56}$	Galtsoff (1966)

Notes: All models are functions of size, x (mm). The scaling relationship for shell parameters converts length, in mm, to a surface area, in m^2 . Predicted values for growth (\hat{y}) are the log change in size given current size. Values in parentheses are standard errors of parameter estimates.

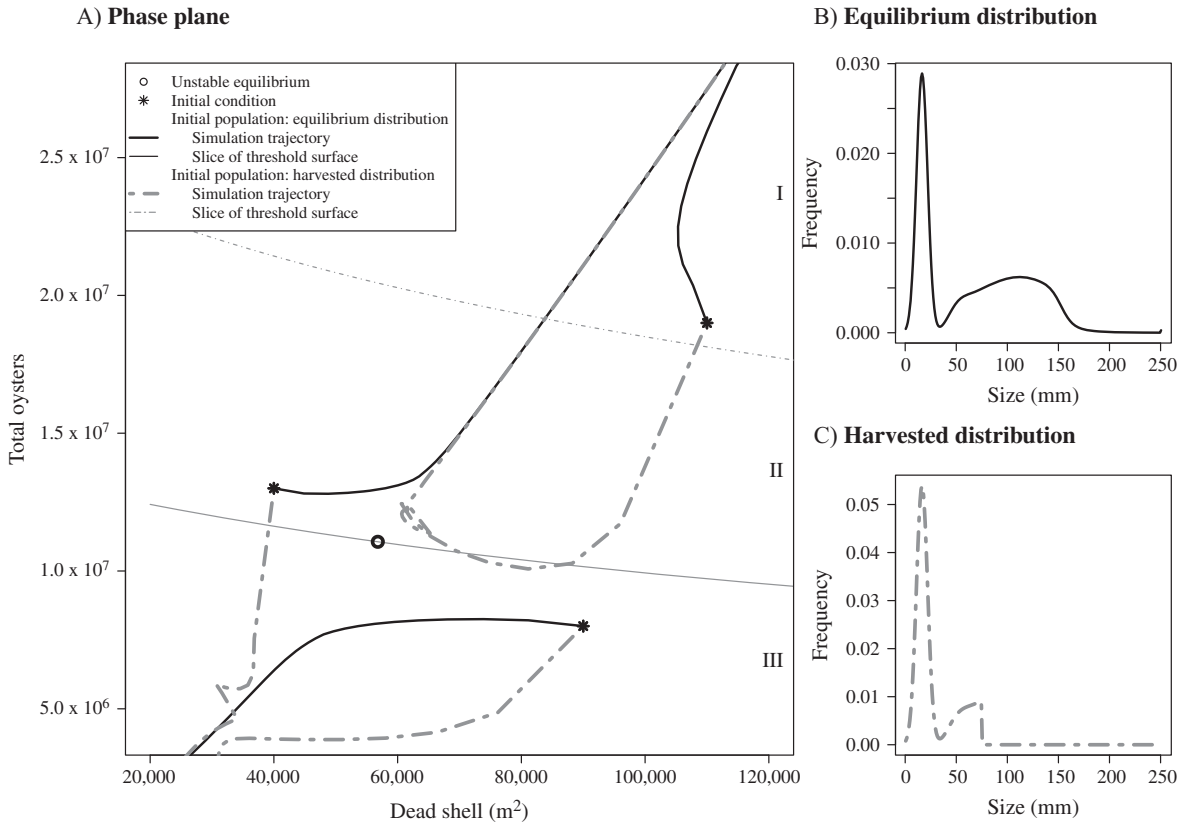


FIG. 4. Population trajectories and initial size distributions. (A) Population trajectories in the absence of restoration for ρ_{low} with remaining parameters given in Table 1. Populations begin at either the equilibrium size distribution (B; thick black lines), or a harvested size distribution (C; thick gray lines). Black stars indicate initial conditions, while the black circle indicates the unstable equilibrium, (\bar{N}, \bar{H}) . Thin lines give the slice of threshold surface corresponding to the equilibrium size distribution (solid black), or the harvested size distribution (dotted gray). Above the slice for the harvested distribution (region I), populations beginning at either size distribution will increase to infinity, while below the slice for the equilibrium distribution (region III), populations beginning at either size distribution will decline to extinction. Between these two slices of the threshold surface (region II), populations beginning at the equilibrium size distribution will increase to infinity, while populations beginning at the harvested size distribution will decline to extinction. (B) The size distribution of the population at equilibrium (when $\lambda = 1$ in the linear model). (C) The size distribution of a harvested population, obtained by truncating the equilibrium size distribution such that all oysters ≥ 75 mm are removed from the population.

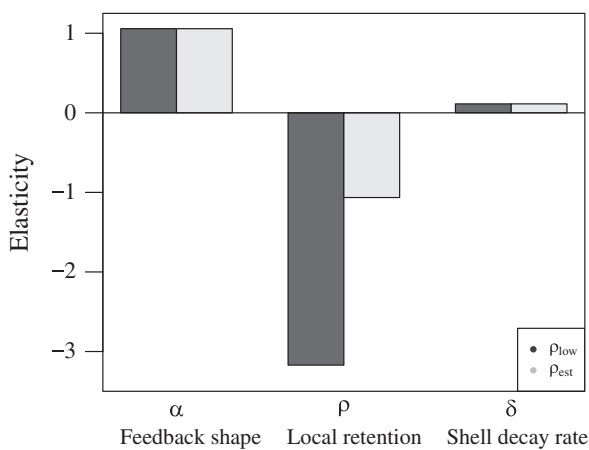


FIG. 5. Elasticity analysis. Elasticity of equilibrium oyster numbers for ρ_{low} (dark bars) and ρ_{est} (light bars), with remaining parameters given in Table 1. The elasticity of equilibrium dead shell levels is the same as the elasticity of equilibrium oyster numbers for α and ρ . The elasticity of \bar{H} to δ is equal to -0.0683 for ρ_{low} and ρ_{est} .

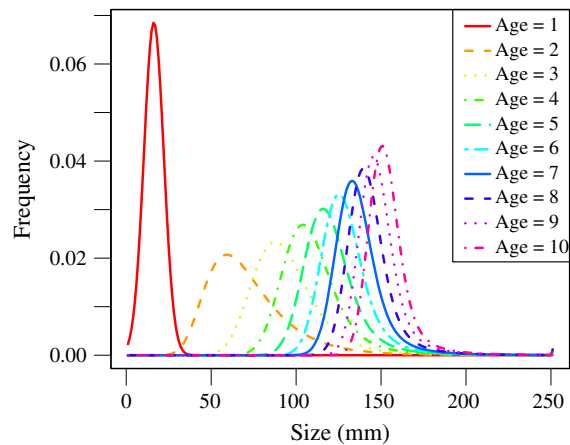


FIG. 6. Age-specific size distributions for *Crassostrea virginica*. Size distributions for each age from $a = 1$ to $a = 10$. Distributions are generated by applying the growth and survival kernels to an initial distribution of new $a = 1$ recruits and normalizing the distribution after each time step.

the methods presented in Appendix S4, we analytically approximate the total number of oysters of a particular age cohort that are required to cross the threshold surface. These results, as well as the results of the numerical simulations, are shown in Fig. 7A.

For all parameter combinations evaluated, the greatest number of oysters are required if oysters are added to the system at age 1, while the fewest number of oysters are required if oysters are added to the system between the ages of 3–7. When local retention, ρ , is low, significantly more oysters are required to push the population across the threshold surface, vs. when ρ is high. Increasing δ increases \hat{N} and thus the overall number of oysters required to cross the threshold.

While the analytic approximations work well, in general they slightly underestimate the number of oysters required (Fig. 7B). When δ is low, the underestimation becomes more pronounced.

The degree of effort required for habitat enhancement depends upon the initial population size and size distribution of the population (Fig. 8). If ρ is low, more dead shell substrate is required to push the population over the threshold surface, vs. when ρ is high. If the population begins at its equilibrium size distribution, with total oyster numbers above \hat{N} but no dead shell substrate, the amount of additional substrate required is less than the equilibrium value of dead shell (Fig. 8A). However, if the population begins below \hat{N} , or at a size distribution similar to that of a harvested population, significantly more additional substrate is required beyond the equilibrium value (Fig. 8B).

DISCUSSION

We found that incorporating positive density dependence into a size- and age-structured IPM can create an infinite

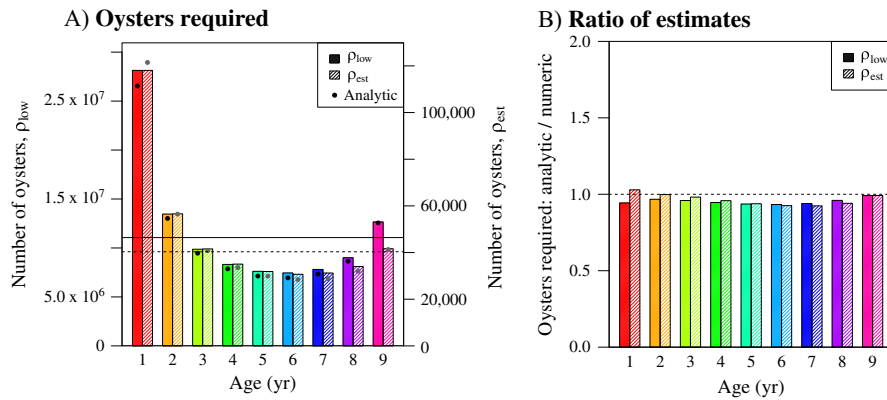


FIG. 7. Oyster additions required for restoration. (A) The number of oysters of a single age, a , needed to push the population across the threshold surface for ρ_{low} (solid bars, left axis), and ρ_{est} (shaded bars, right axis), with remaining parameters given in Table 1. Horizontal lines indicate the equilibrium total oyster number, \hat{N} , for ρ_{low} (solid), and ρ_{est} (dotted). Black and gray points indicate the analytic approximation of required oysters for ρ_{low} and ρ_{est} , respectively. All populations began with no available substrate, and no oysters. (B) The ratio of the required number of oysters calculated from the analytic approximation to the required number of oysters generated from numeric simulations for each age a for ρ_{low} (solid bars, left axis), and ρ_{est} (shaded bars, right axis). The horizontal line indicates a perfect correspondence between the two values, while bars above or below this line indicate an over- or under-estimation of the analytic approximation, respectively.

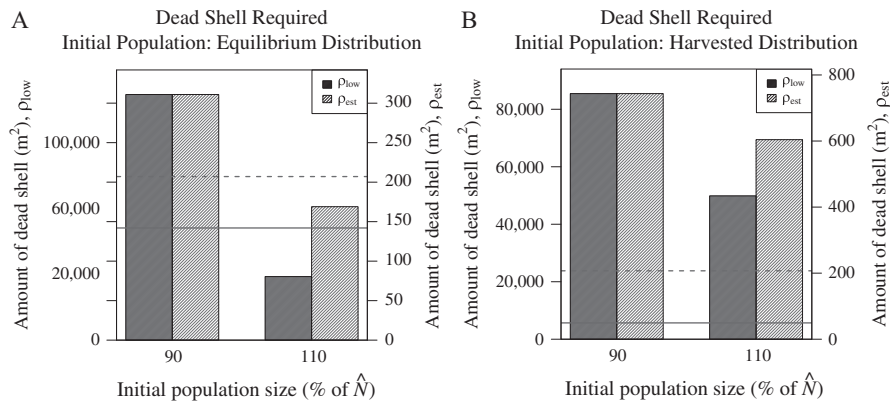


FIG. 8. Dead shell additions required for restoration. The amount of dead shell required to push the population across the threshold surface for ρ_{low} (solid bars, left axis), and ρ_{est} (shaded bars, right axis), with remaining parameters given in Table 1. Horizontal lines indicate the equilibrium total dead shell surface area, \hat{H} , for ρ_{low} (solid), and ρ_{est} (dotted). All populations began at either 90% or 110% of \hat{N} , with the initial size distribution of the population set at (A) the equilibrium size distribution or (B) the harvested size distribution.

dimensional threshold surface below which the population would decline to extinction, and above which the population would increase to infinity. This surface existed when $\rho > \hat{\rho}$. That is, when positive feedbacks are included in the model, the maximum degree of local retention must be greater than if positive feedbacks are not considered, since the feedback term scales the number of recruits, and decreases recruitment when \hat{H} and \hat{N} are low.

Additionally, we found that population dynamics near the threshold surface were highly dependent upon the size and age distribution of the population. This is because the threshold not only depends on the total oyster numbers and substrate levels, but also on the size and age distribution. As such, even if the total number of oysters in the population exceeds the total equilibrium oyster number, \hat{N} , the number of oysters of a particular size and age might be below the threshold surface, and the population might still decline to extinction. For example, in a population that has experienced significant harvest pressure and only oysters <75 mm shell length remained in the population, the total number of oysters and dead shell had to be well above \hat{N} and \hat{H} in order for the population to persist. While our results indicate the existence of a restoration threshold that must be met for successful restoration (Suding and Hobbs 2008), our results also emphasize the complexity of this threshold. It thus becomes particularly important to set a desired size- and age-structure as a goal of restoration, and not just an overall number of oysters or substrate (Baggett et al. 2014, 2015, Moore et al. 2016). In addition, in simulations that began away from the equilibrium size- and age-structure, populations exhibited oscillatory dynamics for upwards of 10 yr, both when declining to extinction or persisting. When monitoring real world oyster populations, this indicates the potential difficulty of using short time series observations to judge the need for, or the success of, restoration actions, as populations in the declining phase of an oscillation may ultimately persist.

The location of the threshold surface is dependent upon parameters whose estimates are highly uncertain. The threshold surface was most affected by changes in ρ , the maximum degree of local retention, with increases in ρ leading to decreases in the location of the threshold surface. That is, if more oyster recruits survive and remain in the natal population, the smaller the extinction region, and thus the increased likelihood of a persistent population. In terms of restoration, this supports the idea that restoration should focus on locations with a high degree of local retention or larval survival. This could be achieved by assessing the abiotic conditions of the region, such as salinity or specific hydrodynamic patterns, as well as focusing on areas of low predation and disease.

Alternatively, increases in both δ and α led to increases in the threshold surface, making it less likely that the population would persist. Increases in δ , the decay rate of shell substrate, indicate that the substrate will not persist as long in the system, and thus there will be less overall recruits that are able to successfully establish. This is of particular importance as there is evidence that climate change will increase ocean acidification (Orr et al. 2005, Gaylord et al. 2015). Increases in ocean acidification will decrease the calcification of oyster shells, making the shell weaker and ultimately increasing shell erosion rates (i.e., increasing δ ; Waldbusser et al. 2011).

Additionally, δ is temporally and spatially variable (Powell et al. 2006, Wilberg et al. 2013). For instance, natural bioeroders such as boring sponge (*Cliona* spp.), which may increase shell decay rate, are more prevalent in higher salinity area (Dunn et al. 2014). Given that, restoration actions should again focus on particular locations where δ is low, or adapt restoration actions to local environmental conditions.

The α parameter determines the shape of the feedback function; high values of α decrease the strength of the positive feedback (thus increasing the equilibrium value and making it more difficult to push the population across the threshold surface), while low values of α increase the strength of the positive feedback. When restoring populations, there are many ways that substrate is added to existing populations. Loose shell can be dumped across large regions of the population, shells can be bagged first before being placed, or large artificial structures can be built and added to the population (Brumbaugh and Coen 2009, Theuerkauf et al. 2015). This analysis supports the idea that the most effective technique will be the one that best facilitates oyster recruitment. While there is some data on the relationship between substrate and recruitment (Colden et al. 2017), much is still unknown, and oyster restoration efforts would likely benefit from additional studies investigating this relationship.

Additionally, our analysis shows that approximately three times as many oysters are required if spat are added to the system, rather than larger, mid-aged oysters. This might explain why seeding oysters is not always successful at enhancing oyster populations (e.g., Geraldi et al. 2013, Puckett and Eggleston 2016). When seeding oyster populations, oyster larvae are grown on recycled shell in the lab, and then planted in the natural population once they reach a large enough size to limit mortality (Brumbaugh and Coen 2009). As oysters grow older and larger, it becomes cost prohibitive to continue rearing the oysters in the lab. However, our results indicate that it would be worthwhile to consider methods of growing oysters to a larger size in a stress-free, high survival environment before planting them in a degraded location where restoration is desired. This could involve transplanting oysters from protected sites, or coordinating with aquaculture or community-based oyster gardening facilities.

A coupled ecological and economic modeling study conducted by Kellison and Eggleston (2004) for summer flounder stock enhancement found similar results: the number of survivors of released stock was maximized, and the total cost per survivor was minimized, when fish were released at the maximum size possible. A similar cost-benefit analysis could be done for oysters that incorporates the cost of growing a given number of oysters to a particular size to better determine the most economic size and age of oysters to use for restoration. Additionally, while this analysis looked at the minimum level of stock enhancement required for persistence, future work could also incorporate an “economic restoration threshold” (Lampert and Hastings 2014) to determine the optimal level of stock enhancement (which might exceed the minimum level) required to meet a restoration goal in a cost-effective manner.

For substrate addition, an unrealistic amount of dead shell (>40 million m²) was required if the population began at low (<10% of \hat{N}) population levels and ρ_{low} (results not shown). If the population began close to the equilibrium

total oyster numbers, the amount of dead shell required was closer to more reasonable levels. However, if ρ was low or δ was high, substantially more substrate was required. The initial size distribution of the population was also important. If the population began at the equilibrium size distribution, then the amount of dead shell required was less than the equilibrium level if the population began at 110% of \hat{N} , while the amount was greater than the equilibrium level if the population began at 90% of \hat{N} . However, if the population began with a size distribution similar to that of a harvested population, even if the population began above the equilibrium number of total oysters, significantly more dead shell beyond the equilibrium levels was required to restore the population. This result reinforces the idea that the structure of the population is of equal importance as the overall size of the population for a healthy, persistent population (Baggett et al. 2014, 2015, Moore et al. 2016).

The analytic approximation of oysters required tended to slightly underestimate the number of oysters required, particularly when δ is low. However, within the range of parameter values explored, the analytic approximation was within 25% of the numeric value. Given the high dimension of the threshold surface, it is surprising that the analytic approximation performs this well. This success of the analytical approach suggests that it might be useful for other IPMs and matrix models with positive feedbacks.

Limitations and challenges

Our model, which includes both structuring population variables and positive density dependence, allows for direct assessment of the required number of oysters or substrate for a persistent population. However, there are several important factors that are not yet incorporated into the model presented here. First, we only include positive feedbacks in the fecundity term of the model. In reality, the amount of substrate will also have a positive effect on adult oyster growth and survival, for example, through the interaction between reef height and shape, water depth, and water flow speeds (Lenihan and Peterson 1998, Bartol et al. 1999, Lenihan 1999, Jordan-Cooley et al. 2011). Additionally, the three-dimensional shape of a reef plays a role in determining how much of the overall shell surface area is available for settlement. Future work could extend the IPM presented here to include a variable for reef height or shape, or a structuring variable that represents the location of individual oysters within the reef. Model extensions could also include processes such as oyster filtration of sediment, and a variable to describe sediment dynamics, as has been included in other oyster models (Jordan-Cooley et al. 2011). This will likely significantly increase the complexity of the dynamics.

Our model also does not include negative density dependence, which is important for oyster dynamics (Knights and Walters 2010, Puckett and Eggleston 2012). However, preliminary analysis of a model with both positive and negative feedbacks on fecundity indicate that, with the exception of a positive stable equilibrium surface in addition to the unstable threshold equilibrium surface, qualitative results are similar. Additionally, since we are focused on restoring highly degraded populations, population sizes are likely too small for negative density dependence to have a large effect.

Next, our model assumes a closed population with no external subsidy of recruits. Because of this, any new oysters must either be generated by the local population, or added through restoration actions. This likely explains the unrealistic amount of additional dead shell required at low population sizes. Though many natural oyster reefs are fairly isolated, such as the site used to parameterize the model, many natural oyster reefs receive a large proportion of recruits from external populations, and even isolated populations likely receive some larvae from external sources (Lipcius et al. 2008, 2011, 2015, Puckett and Eggleston 2016). Future work could extend the model to allow for external recruitment to better understand how external subsidies affect the location of the threshold surface. Additionally, the inclusion of external recruitment into future models can give managers a better sense for the relative effectiveness of either stock or habitat enhancement.

Finally, model parameters ρ , δ , and α are highly uncertain, and also highly variable in space and time. While qualitative results do not differ significantly across the range of parameter values explored, if managers are interested in determining more precisely the location of the threshold surface, more accurate parameter estimates are needed. In most cases, managers will not have a firm grasp on any of the three parameters, but based on our elasticity analysis, obtaining accurate estimates of local retention should be prioritized followed by the relationship between substrate and recruitment, and the local substrate decay rates. Additionally, to incorporate variability in model parameters, future work could extend the model to allow for stochasticity, particularly in fecundity and recruitment, which is highly variable both within and between years (Cox and Mann 1992, Ortega and Sutherland 1992, Siegel et al. 2008, Mroch et al. 2012). Last, the model implements a restoration strategy in year 1 of a 150 yr time line. Future work could investigate restoration actions over multiple years, as well as simultaneous substrate and oyster addition.

CONCLUSION

Using demographic data from a population of eastern oyster, *C. virginica*, in Pamlico Sound, North Carolina, our modeling analysis indicates the importance of positive density dependence at influencing population dynamics. We show how population parameters, such as local retention and the decay rate of shell substrate, influence the amount of restoration needed to restore a degraded population. We find that if mid-aged oysters are used for stock enhancement of fully degraded populations, fewer numbers are required for restoration than if oyster spat are used. Finally, we find that restoration of existing populations depends strongly upon the initial size distribution of the population. Future work allowing for external recruitment is needed to better investigate the relative importance of stock enhancement vs. habitat enhancement.

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